

Cambridge IGCSE[™]

CAMBRIDGE INTERNATIONAL MATHEMATICS Paper 6 Investigation and Modelling (Extended) MARK SCHEME B Maximum Mark: 50

Specimen

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptions for the question
- the specific skills defined in the mark scheme or in the generic level descriptions for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptions.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptions in mind.

Mathematics-Specific Marking Principles

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to help with understanding of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Types of mark

- M Method mark, awarded for a valid method applied to the problem.
- A Accuracy mark, given for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- **B** Mark for a correct result or statement independent of Method marks.
- C Communication mark, for clear mathematical communication and reasoning.

Abbreviations

awrt answers which round to cao correct answer only

dep dependent on the previous mark(s)

FT follow through after error

isw ignore subsequent working (after correct answer obtained)

nfww not from wrong working

oe or equivalent SC special case soi seen or implied

Section A

| Question | Answer | Marks | Partial Marks |
|----------|---|-------|---|
| 1(a) | 34 isw | 1 | |
| 1(b) | 34 + 36 | C1 | FT their 34 |
| | 70 | 1 | FT their 34 |
| 2(a) | $a^2 + b^2$ | 1 | |
| 2(b) | $d^2 = PR^2 + c^2$ leading to $d^2 = a^2 + b^2 + c^2$ | 1 | |
| 3 | $4^2 + 17^2 + 28^2$ [= 1089] | 1 | |
| | $\sqrt{their 1089}$ | 1 | |
| | (4, 17, 28, 33) | 1 | |
| 4(a) | $18^2 + 24^2 + 72^2$ | C1 | |
| | (18, 24, 72, 78) | 1 | |
| 4(b) | $(ka)^2 + (kb)^2 + (kc)^2 = (kd)^2$ | 1 | |
| | $k^{2}a^{2} + k^{2}b^{2} + k^{2}c^{2} = k^{2}d^{2}$ leading correctly to $a^{2} + b^{2} + c^{2} = d^{2}$ | 1 | |
| 4(c) | Divide by 6 or common factor = 6 oe | C1 | Accept division by both 2 and 3 |
| | (3, 4, 12, 13) | 1 | FT (18, 24, 72, 72) giving (3, 4, 12, 12) or (18, 24, 72, 84) giving (3, 4, 12, 14) or (18, 24, 72, 90) giving (3, 4, 12, 15) |
| 5(a) | $(a+c)^2 = a^2 + 2ac + c^2$ soi oe | 1 | |
| | $b^2 = 2ac$ leading to $ac = \frac{b^2}{2}$ | 1 | |

Cambridge IGCSE – Mark Scheme SPECIMEN

| Question | Answer | Marks | Partial Marks |
|----------|---|-------|---|
| 5(b) | Since ac is an integer then $\frac{b^2}{2}$ is an integer oe So b^2 is even and then b is even | 2 | M1 for ac is an integer then $\frac{b^2}{2}$ is an integer oe A1 dep for so b^2 is even, then b is even |
| | Alternative | (2) | |
| | If b is odd, then b^2 is odd | | M1 for b is odd then b^2 is odd so $\frac{b^2}{2}$ is not an integer |
| | so $\frac{b^2}{2}$ is not an integer then ac is not an integer | | A1 dep for then ac is not an integer |
| 6 | $\frac{8^2}{2}$ | C1 | |
| | ac = 32 | 1 | |
| | 1 and 32 2 and 16 4 and 8 | C1 | |
| | Substitution of one of <i>their</i> pairs into $a + c$ or $a^2 + 8^2 + c^2$ oe | C1 | |
| | (1, 8, 32, 33) (1, 4, 8, 9) (1, 2, 2, 3) | 3 | B1 for each or B2 for (1, 8, 32, 33), (2, 8, 16, 18), (4, 8, 8, 12) which may be implied by <i>d</i> = 33, 18 and 12 seen |

Section B

| Question | Answer | Marks | Partial Marks |
|----------|--|------------|---|
| 7(a) | $\frac{20}{50} \times 60$ soi oe | C2 | C1 for $\frac{20}{50}$ or for \times 60 |
| | 24 [minutes] | 1 | |
| 7(b) | $m = \frac{1200}{v}$ | 1 | |
| 8(a)(i) | 20 seen | C 1 | |
| | 30 km/h | 1 | FT 50 – their 20 |
| 8(a)(ii) | $\frac{1200}{30} = 40$ | 1 | Accept 20 × 60 for 1200 |
| | $\frac{20}{30} = \frac{2}{3}$ hours = 40 | | |
| 8(b) | $50 - \frac{x}{2}$ seen | 1 | |
| | $T = \frac{1200}{50 - \frac{x}{2}} \text{ leading to } T = \frac{2400}{100 - x}$ | 1 | Accept 20 × 60 for 1200 |

| Question | Answer | Marks | Partial Marks |
|----------|--|-------|--|
| 8(c) | Correct sketch T 0 0 0 0 0 0 0 0 0 0 0 0 | 1 | |
| | T intercept marked as 24 | C1 | |
| 8(d) | T = 30 drawn on the graph or $\frac{2400}{100 - x} = 30$ | C1 | Allow inequality |
| | 7.20[am] oe | 1 | |
| 8(e)(i) | $\frac{2400}{100 - 95}$ or $x = 95 \text{ seen on graph of } T = \frac{2400}{100 - x}$ | C1 | P1 for 9 hours or 490 minutes |
| | 7h 35 min | 2 | B1 for 8 hours or 480 minutes FT their 95 if between 60 and 100 |

| Question | Answer | Marks | Partial Marks |
|-----------|---|-------|---|
| 8(e)(ii) | Not useful for leaving home very late oe | 1 | For 'very late' accept times from 8.15 am onwards |
| | or | | |
| | unsuitable for 100 minutes after 7.00 am oe | | |
| 9(a) | number of minutes after 7.00 am + time to drive to work oe | 1 | |
| 9(b)(i) | $x + \frac{2400}{100 - x} = 120$ | 1 | |
| | Correct elimination of fractions | 1 | e.g. $x(100 - x) + 2400 = 120(100 - x)$ |
| | Correct expansion of brackets leading to $x^2 - 220x + 9600 = 0$ nfww | 1 | |
| 9(b)(ii) | Sketch of $y = x^2 - 220x + 9600$ with left positive intercept clearly marked | C2 | C1 for sketch of $y = x^2 - 220x + 9600$ with both x-intercepts positive. |
| | or $(x-60)(x-160)$ | | or C1 for $(x + a)(x + b)$ where $ab = 9600$ or $a + b = -220$ or for 60 and 160 with wrong signs |
| | or $\frac{(-220) \pm \sqrt{(-220)^2 - 4 \times 9600}}{2} = 60, 160$ | | or C1 for $\frac{(-220) \pm \sqrt{(-220)^2 - 4 \times 9600}}{2}$ or better |
| | or at least two trials, one of which is 60. | | or C1 for $60^2 - 220 \times 60 + 9600$ |
| | 60 | 1 | Including 160 scores 0 |
| 9(b)(iii) | 8 am oe | 1 | FT their 60 |

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